## To the Student

## **Investigation 0: Random babies**

# **CHAPTER 1: ANALYZING STATISTICAL PROCESSES**

In this chapter, you will begin to analyze results from statistical studies and focus on the process of statistical inference. In particular, you will learn how to assess evidence against a particular claim about a random process.

Section 1: Analyzing a process probability

Investigation 1.1: Friend or foe – Inference for a proportion Probability Exploration: Mathematical model Investigation 1.2: Do names match faces – Bar graph, hypotheses, binomial test (technology) Investigation 1.3: Heart transplant mortality – Factors affecting p-value Investigation 1.4: Kissing the right way – Two-sided p-values Investigation 1.5: Kissing the right way (cont.) – Interval of plausible values Investigation 1.6: Improved batting averages – Types of error and power Probability Exploration: Exact Binomial Power Calculations

Section 2: Normal approximations for sample proportions

Investigation 1.7: Reese's pieces – Normal model, empirical rule, CLT Investigation 1.8: Is ESP real? – Normal probabilities, *z*-score Investigation 1.9: Halloween treat choices – Test statistic, continuity correction Investigation 1.10: Kissing the right way (cont.) – *z*-interval, confidence level Investigation 1.11: Heart transplant mortality (cont.) – Adjusted Wald

## Section 3: Sampling from a population

Investigation 1.12: Sampling words – Biased and random sampling Investigation 1.13: *Literary Digest* – Issues in sampling Investigation 1.14: Sampling words cont. – Central Limit Theorem for  $\hat{p}$ Investigation 1.15: Freshmen voting pattern – Nonsampling errors, hypergeometric Investigation 1.16: Teen hearing loss – One sample *z*-procedures Investigation 1.17: Cat households – Practical significance Investigation 1.18: Female senators – Cautions in inference

Example 1.1: Predicting Elections from Faces

Example 1.2: Cola Discrimination

Example 1.3: Seat Belt Usage

Appendix: Stratified random sampling

# **CHAPTER 2: COMPARING TWO PROPORTIONS**

In this chapter, you will focus on comparing results from two groups on a categorical variable. These groups could be samples from different populations or they could have been deliberately formed during the design of the study. You will again consider different ways to analyze the statistical significance of the difference in the groups, namely simulation, exact methods, and normal approximations to answer whether the observed difference in the groups could have happened "by chance alone." You will also continue to consider issues of statistical confidence and types of errors. A key consideration to keep in mind will be the scope of conclusions that you can draw from the study based on how the data were collected.

## Section 1: Comparing two population proportions

Investigation 2.1: Teen hearing loss (cont.) – Tables, conditional props, bar graphs, *z*-procedures Investigation 2.2: Night Lights and Near-sightedness – Association, confounding

## Section 2: Types of Studies

Investigation 2.3: Handwriting and SAT scores – Observational studies, experiments Investigation 2.4: Have a nice trip – Random assignment, scope of conclusions Investigation 2.5: Botox for back pain – Designing experiments

## Section 3: Comparing two treatment probabilities

Investigation 2.6: Dolphin Therapy – Randomization test Investigation 2.7: Is yawning contagious? – Fisher's exact test Investigation 2.8: CPR vs. chest compressions – z-procedures

## Section 4: Other Statistics

Investigation 2.9: CPR vs. chest compressions – Relative risk Investigation 2.10: Smoking and lung cancer – Types of observational studies, odds ratio Investigation 2.11: Sleepy drivers – Odds ratio confidence interval

Example 2.1: Wording of Questions

Example 2.2 Worries about Terrorist Attacks

# **CHAPTER 3: COMPARISONS WITH QUANTITATIVE VARIABLES**

This chapter parallels the previous one in many ways. We will continue to consider studies where the goal is to compare a response variable between two groups. The difference here is that these studies will involve a *quantitative* response variable rather than a *categorical* one. The methods that we employ to analyze these data will therefore be different, but you will find that the basic concepts and principles that you learned in Chapters 1 and 2 still apply. These include the principle of starting with numerical and graphical summaries to explore the data, the concept of statistical significance in determining whether the difference in the distribution of the response variable between the two groups is larger than we would reasonably expect from randomization alone, and the importance of considering how the data were collected in determining the scope of conclusions that can be drawn from the study.

Section 1: Quantitative data

Investigation 3.1: How faithful is Old Faithful? – Descriptive statistics Investigation 3.2: The *Ethan Allen* – Sampling distributions for  $\bar{x}$ Investigation 3.3: Healthy body temperatures – Student's *t*-distribution Investigation 3.4: Healthy body temperatures (cont.) – *t*-procedures, prediction intervals

Section 2: Comparing two population means

Investigation 3.5: Left-handedness and life expectancy – Random sampling, 2-sample *t*-tests Investigation 3.6: Left-handedness and life expectancy (cont.) – Application, Power

Section 3: Comparing two treatment means

Investigation 3.7: Lingering effects of sleep deprivation – Randomization tests Investigation 3.8: Lingering effects of sleep deprivation (cont.) – two-sample *t*-tests Investigation 3.9: Ice cream serving sizes – two-sample *t*-confidence interval Investigation 3.10: Cloud seeding – Strategies for non-normal data

#### Section 4: Matched Pairs Designs

Investigation 3.11: Chip melting times – Independent vs. paired design, technology Investigation 3.12: Chip melting times (cont.) – Inference (simulation, paired *t*-test) Investigation 3.13: Comparison shopping – Application Investigation 3.14: Smoke alarms – McNemar's test (paired categorical data)

Example 3.1: Age Discrimination – Exact randomization test

Example 3.2: Speed Limit Changes – Two-sample *t*-test

Example 3.3: Distracted Driving? – Matched pairs

Example 3.4: Distracted Driving (cont.) – Sign test

## **CHAPTER 4: COMPARING SEVERAL POPULATIONS, EXPLORING RELATIONSHIPS**

The idea of comparing two groups has been a recurring theme throughout this course. In the previous chapters, you have been limited to exploring two groups at a time. You saw that often the same analysis techniques apply whether the data have been collected as independent random samples or from a randomized experiment, although this data collection distinction strongly influences the scope of conclusions that you can draw from the study. You will see a similar pattern in this chapter as you extend your analyses to exploring two or more groups. In particular, you will study a procedure for comparing a categorical response variable across several groups and a procedure for comparing a quantitative response variable across several groups. You will also study the important notion of association between variables, first with categorical variables and then for studies in which both variables are quantitative. In this latter case, you will also learn a new set of numerical and graphical summaries for describing these relationships.

#### Section 1: Two Categorical Variables

Investigation 4.1: Dr. Spock's Trial – Chi-square test for homogeneity of proportions Investigation 4.2: Near-sightedness and night lights (cont.) – Chi-square test for association Technology Exploration: Randomization test for chi-square statistic Investigation 4.3: Newspaper credibility decline – Comparing distributions

#### Section 2: Comparing Several Population Means

Investigation 4.4: Disability discrimination – Reasoning of ANOVA Applet Exploration: Randomization test for ANOVA Investigation 4.5: Restaurant spending and music – ANOVA practice Applet Exploration: Exploring ANOVA

#### Section 3: Two Quantitative Variables

Investigation 4.6: Cat jumping – Scatterplots Investigation 4.7: Drive for show, putt for dough – Correlation coefficients Applet Exploration: Correlation guessing game Investigation 4.8: Height and foot size – Least squares regression Applet Exploration: Behavior of regression lines – Resistance Excel Exploration: Minimization criteria Investigation 4.9: Money-making movies – Application

## Section 4: Inference for Regression

Investigation 4.10: Running out of time – Inference for regression (sampling) Investigation 4.11: Running out of time (cont.) – Inference for regression (shuffling) Investigation 4.12: Boys' heights – Regression model Investigation 4.13: Cat jumping (cont.) – Confidence intervals for regression Investigation 4.14: Housing prices – Transformations Technology Exploration: The regression effect

Example 4.1: Internet Use by Region

Example 4.2: Lifetimes of Notables

Example 4.3: Physical Education Class Performance

**Example 4.4: Comparing Population Diets**