

Practice:

4-14) Swain v. Alabama

In *Swain v. Alabama* (1965) it was alleged that there was discrimination against blacks in grand jury selection. Swain, a black man, was convicted in Talladega County, Alabama, of raping a white woman and was sentenced to death. At that time in Alabama, only men over the age of 21 were eligible for jury duty. Census data suggested that about 26% of those eligible for grand jury service were black, yet a “random sample” of 1050 individuals called to appear for possible grand jury duty yielded only 177 blacks.

- (a) Produce numerical and graphical summaries of the sample results.
- (b) Define the parameter of interest.
- (c) State the null and alternative hypotheses.
- (d) Describe what a Type I Error and a Type II Error would represent in this situation. What are the consequences of each type of error?
- (e) Is the normal model valid here? If so, use the central limit theorem to calculate the test statistic and p-value (include a sketch). If not, calculate the p-value based on the binomial distribution.
- (f) Do you reject or fail to reject the null hypothesis based on this p-value? The Supreme Court ruled that this disparity was small. Do you agree with this decision?

4-15) Cat Ownership

A survey of 80,000 households conducted by the American Veterinary Medical Association in 1996 found 27.3% of households reported that they owned a pet cat.

- (a) State (in words and in symbols) the hypotheses for testing whether the sample data provide strong evidence that the proportion of all households that own a pet cat *differs* from .25. *Hint: Think two-sided.*
- (b) Use the central limit theorem to calculate the test statistic and a two-sided p-value. State your conclusion about the null hypothesis and about the research question. How strong is the evidence against the null hypothesis?
- (c) Does 27.3% versus 25% seem like a large difference to you in this context?

Discussion: Keep in mind the difference between *statistical significance* and *practical significance*. With large sample sizes, the standard deviation of the sample proportion will be small, and so even small differences will be statistically significant. Saying a sample result is unlikely to happen by chance is not the same as saying the result is important or even noteworthy depending on the context involved.